

Addition

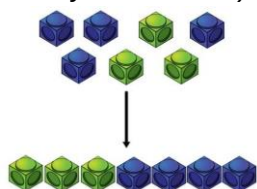
Addition - Key Language

Sum, add, total, parts and wholes, plus, add, bonds, more, across 10

Concrete

Counting and adding more

Children add one more person or object to a group to find one more.



Pictorial

Counting and adding more

Children add one more cube or counter to a group to represent one more.

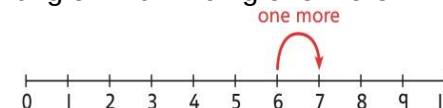


One more than 4 is 5.

Abstract

Counting and adding more

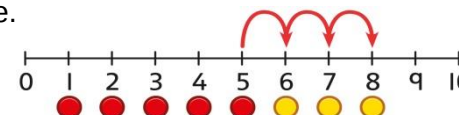
Use a number line to understand how to link counting on with finding one more.



One more than 6 is 7.

7 is one more than 6.

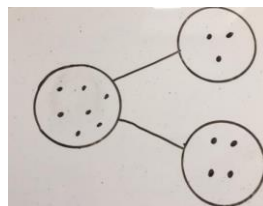
Learn to link counting on with adding more than one.



$$5 + 3 = 8$$

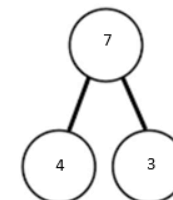
Combining two parts to make a whole (use other resources too e.g. eggs, shells, teddy bears, cars).

Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.



$$4 + 3 = 7$$

Four is a part, 3 is a part and the whole is seven.



Addition

Concrete

Knowing and finding number bonds within 10

Break apart a group and put back together to find and form number bonds.



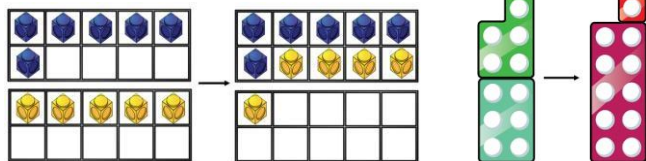
$$3 + 4 = 7$$



$$6 = 2 + 4$$

Regrouping to make 10; using ten frames and counters/cubes or using Numicon.

$$6 + 5$$

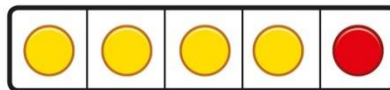


Pictorial

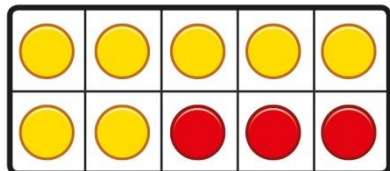
Knowing and finding number bonds within 10

Use five and ten frames to represent key number bonds.

$$5 = 4 + 1$$



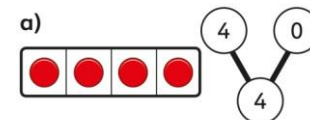
$$10 = 7 + 3$$



Abstract

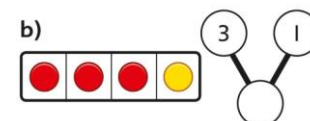
Knowing and finding number bonds within 10

Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.



$$4 + 0 = 4$$

$$3 + 1 = 4$$



Children to develop an understanding of equality e.g.

$$6 + \square = 11$$

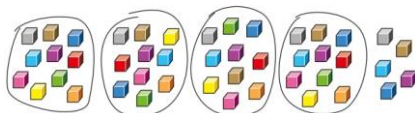
$$6 + 5 = 5 + \square$$

$$6 + 5 = \square + 4$$

Addition

Concrete

Group objects into 10s and 1s.

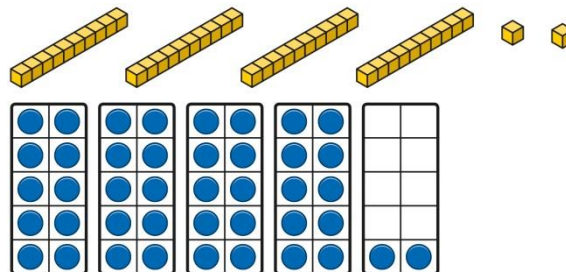


Bundle straws to understand unitising of 10s.



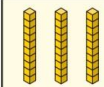
Pictorial

Understand 10s and 1s equipment, and link with visual representations on ten frames.

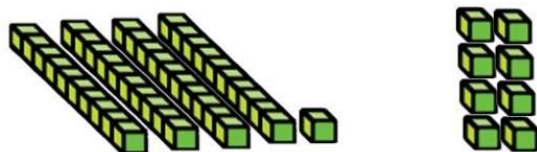


Abstract

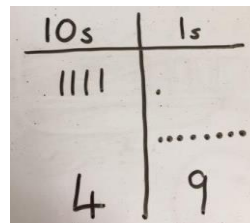
Represent numbers on a place value grid, using equipment or numerals.

Tens	Ones
	
3	2
Tens	Ones
4	3

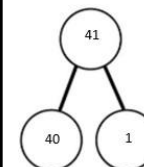
TO + O using base 10. Continue to develop understanding of partitioning and place value.
 $41 + 8$



Children to represent the base 10 e.g. lines for tens and dot/crosses for ones.



$41 + 8$



$$1 + 8 = 9$$

$$40 + 9 = 49$$

	4	1
+		8
	4	9

2 or 3-digit number + 1s with exchange

Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.

Children should explore this using unitised objects or physical apparatus.

Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.

H	T	O
		
H	T	O
		

H	T	O
		
H	T	O
		

$$135 + 7 = 142$$

Understand how to bridge by partitioning to the 1s to make the next 10.

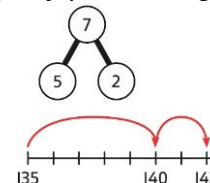
$$135 + 7 = ?$$

$$135 + 5 + 2 = 142$$

Ensure that children understand how to add 1s bridging a 100.

$$198 + 5 = ?$$

$$198 + 2 + 3 = 203$$



Addition

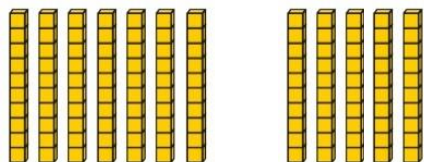
Concrete

Use place value equipment to model addition and understand where exchange is required.

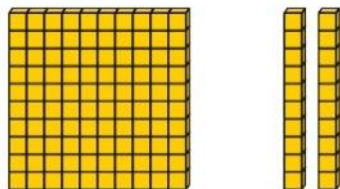
Use place value counters to represent

$$154 + 72.$$

Use this to decide if any exchange is required.



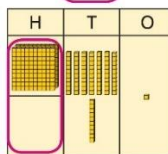
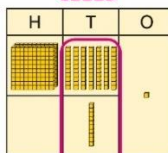
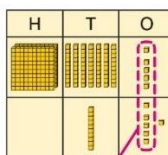
There are 5 tens and 7 tens. That is 12 tens so I will exchange.



Pictorial

Represent the required exchange on a place value grid using equipment.

$$275 + 16 = ?$$



$$275 + 16 = 291$$

Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value.

Children should be encouraged at every stage to select methods that are accurate and efficient.

Abstract

Children must understand how the method relates to place value at each stage of the calculation.

$$\begin{array}{r} \text{H} \text{ T} \text{ O} \\ 2 \ 7 \ 5 \\ + \ 1 \ 6 \\ \hline \end{array}$$

$$\begin{array}{r} \text{H} \text{ T} \text{ O} \\ 2 \ 7 \ 5 \\ + \ 1 \ 6 \\ \hline 9 \ 1 \end{array}$$

$$\begin{array}{r} \text{H} \text{ T} \text{ O} \\ 2 \ 7 \ 5 \\ + \ 1 \ 6 \\ \hline 2 \ 9 \ 1 \end{array}$$

$$275 + 16 = 291$$

Addition

Concrete

Column addition with whole numbers

Use place value equipment to represent additions.

Add a row of counters onto the place value grid to show $15,735 + 4,012$.

TTh	Th	H	T	O
●	●●●●●	●●●●●	●●●●●	●●●●●

Pictorial

Represent additions, using place value equipment on a place value grid alongside written methods.

TTh	Th	H	T	O
●●		●	●●●●●	●●●●●
●●	●●●●●	●	●●●●●	●●●●●

I need to exchange 10 tens for a 100.

TTh	Th	H	T	O
2	0	1	5	3
+	1	9	1	7
3	9	3	2	8

Abstract

Use column addition, including exchanges.

TTh	Th	H	T	O
1	9	1	7	5
+	1	8	4	1
3	7	5	9	2

Adding decimals using column addition

Use place value equipment to represent additions.

Show $0.23 + 0.45$ using place value counters.

Use place value equipment on a place value grid to represent additions.

O	•	Tth	Hth
	•	●●●●●	●●●●●
	•	●●●●●	●●●●●

Represent exchange where necessary.

O	•	Tth	Hth
●●●●●	•		
●	•	●●	●●●●●

Include examples where the numbers of decimal places are different.

Add using a column method, ensuring that children understand the link with place value.

O	•	Tth	Hth
0	•	2	3
+	•	4	5
0	•	6	8

Include exchange where required, alongside an understanding of place value.

O	•	Tth	Hth
0	•	9	2
+	•	3	3
1	•	2	5

Include additions where the numbers of decimal places are different.

O	•	Tth	Hth
3	•	4	0
+	•	6	5

$$3.4 + 0.65 = ?$$

Subtraction

Subtraction - Key Language

Take away, less than, difference, subtract, minus (careful of confusion with directed number), fewer, decrease

Concrete

Counting back and taking away

Children arrange objects and remove to find how many are left.



1 less than 6 is 5.

6 subtract 1 is 5.

Finding the difference

Arrange two groups so that the difference between the groups can be worked out.

8 is 2 more than 6.

6 is 2 less than 8.

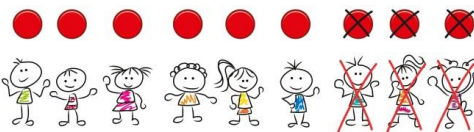


The difference between 8 and 6 is 2.

Pictorial

Counting back and taking away

Children draw and cross out or use counters to represent objects from a problem.

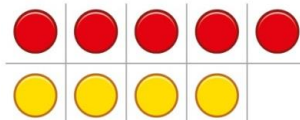


$$9 - \square = \square$$

There are $\square$ children left.

Finding the difference

Represent objects using sketches or counters to support finding the difference.



$$5 - 4 = 1$$

The difference between 5 and 4 is 1.

Abstract

Counting back and taking away

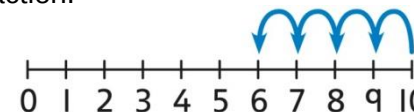
Children count back to take away and use a number line or number track to support the method.



$$9 - 3 = 6$$

Finding the difference

Children understand 'find the difference' as subtraction.



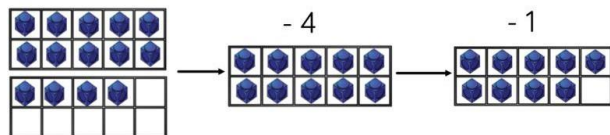
$$10 - 4 = 6$$

The difference between 10 and 6 is 4.

Subtraction

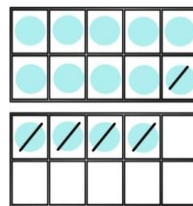
Concrete

Making 10
using ten frames. $14 - 5$



Pictorial

Children to present the ten frame pictorially and discuss what they did to make 10.



Abstract

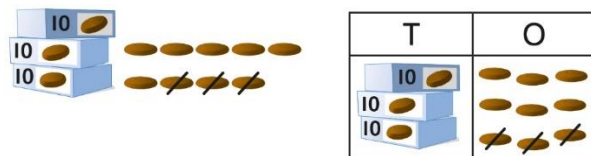
Children to show how they can make 10 by partitioning the subtrahend.

$$\begin{array}{r} 14 - 5 = 9 \\ \swarrow \quad \searrow \\ 4 \quad \quad 1 \end{array}$$

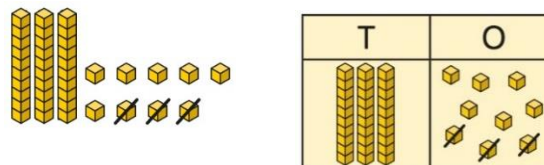
$$\begin{array}{l} 14 - 4 = 10 \\ 10 - 1 = 9 \end{array}$$

Subtracting a single-digit number

Subtract the 1s. This may be done in or out of a place value grid.

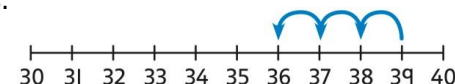


Subtract the 1s. This may be done in or out of a place value grid.



Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds.

$$\begin{array}{r} \text{T} \quad \text{O} \\ 3 \quad 9 \\ - \quad 3 \\ \hline 3 \quad 6 \end{array}$$

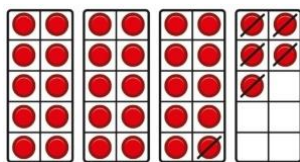


$$9 - 3 = 6$$

$$39 - 3 = 36$$

Bridge 10 by using known bonds.

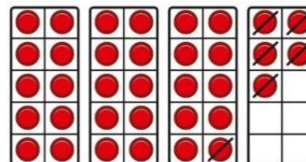
$$35 - 6$$



I took away 5 counters, then 1 more.

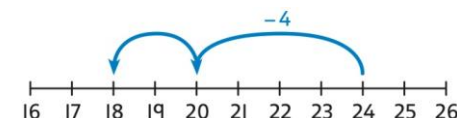
Bridge 10 by using known bonds.

$$35 - 6$$



First, I will subtract 5, then 1.

Bridge 10 by using known bonds.



$$24 - 6 = ?$$

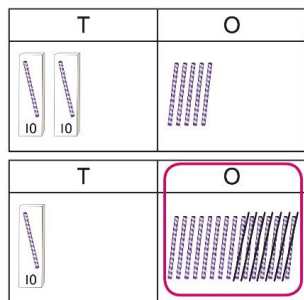
$$24 - 4 - 2 = ?$$

Subtraction

Concrete

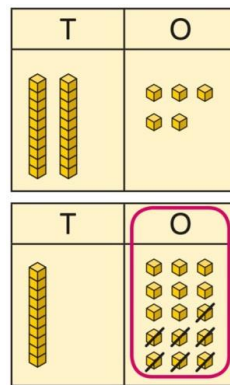
Subtracting a single-digit number using exchange

Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.



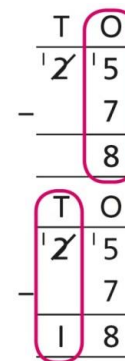
Pictorial

Exchange 1 ten for 10 ones.



Abstract

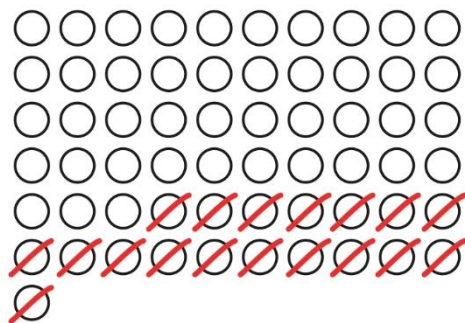
Exchange 1 ten for 10 ones.



$$25 - 7 = 18$$

Subtracting a 2-digit number

Subtract by taking away.



$$61 - 18$$

I took away 1 ten and 8 ones.

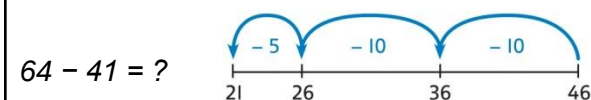
Subtract the 10s and the 1s.

This can be represented on a 100 square.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Subtract the 10s and the 1s.

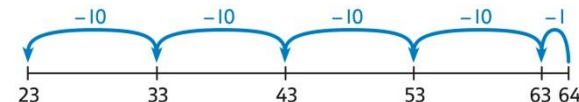
This can be represented on a number line.



$$64 - 1 = 63$$

$$63 - 40 = 23$$

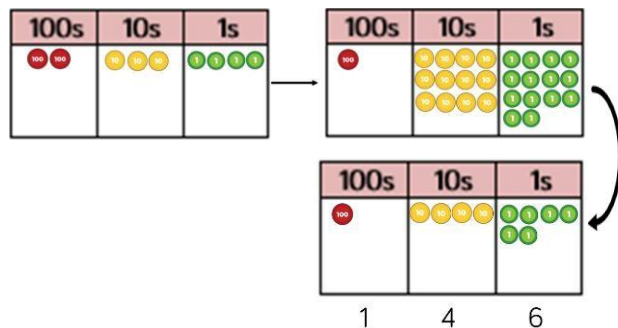
$$64 - 41 = 23$$



Subtraction

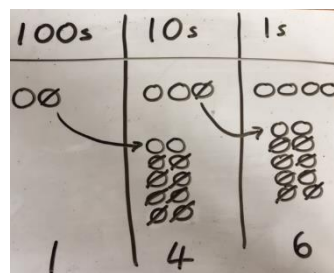
Concrete

Column method using place value counters. $234 - 88$



Pictorial

Represent the place value counters pictorially; remembering to show what has been exchanged.



Abstract

Formal column method. Children must understand what has happened when they have crossed out digits.

$$\begin{array}{r} \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\ 5 \cancel{8} \text{ } \cancel{12} \text{ } 10 \text{ } 9 \text{ } 7 \\ - 1 \text{ } 8 \text{ } 5 \text{ } 3 \text{ } 4 \\ \hline 4 \text{ } 3 \text{ } 5 \text{ } 6 \text{ } 3 \end{array}$$

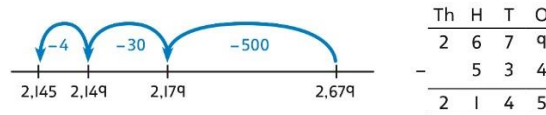
$$62,097 - 18,534 = 43,563$$

Comparing and selecting efficient methods

Use counters on a place value grid to represent subtractions of larger numbers.

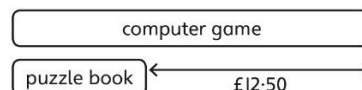
Th	H	T	O

Compare subtraction methods alongside place value representations.



Th	H	T	O

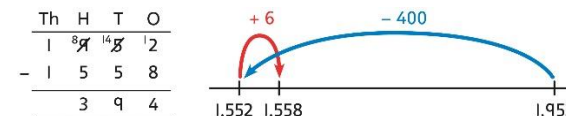
Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.



Compare and select methods.

Use column subtraction when mental methods are not efficient.

Use two different methods for one calculation as a checking strategy.



Use column subtraction for decimal problems, including in the context of measure.

$$\begin{array}{r} \text{H} \text{ T} \text{ O} \cdot \text{Tth} \text{Hth} \\ 3 \text{ } 0 \text{ } 9 \cdot 6 \text{ } 0 \\ - 2 \text{ } 0 \text{ } 6 \cdot 4 \text{ } 0 \\ \hline 1 \text{ } 0 \text{ } 3 \cdot 2 \text{ } 0 \end{array}$$

Multiplication

Multiplication - Key Language

Double, triple, times, multiplied by, product, groups of, lots of, equal groups, multiple

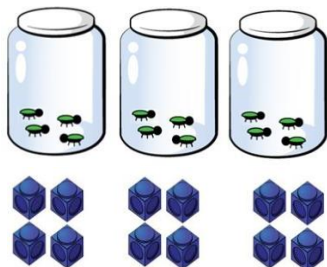
Concrete

**Repeated grouping/
repeated Addition**

$$3 \times 4$$

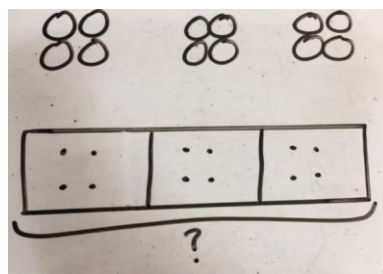
$$4 + 4 + 4$$

There are 3 equal groups, with 4 in each group.



Pictorial

Children to represent the practical resources in a picture and use a bar model.

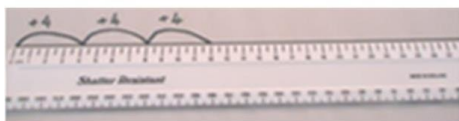


Abstract

$$3 \times 4 = 12$$

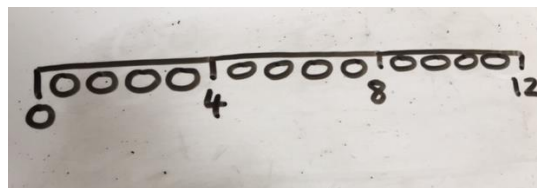
$$4 + 4 + 4 = 12$$

**Number lines to show
repeated groups- 3×4**



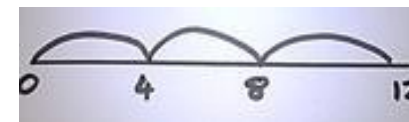
Cuisenaire rods can be used too.

Represent this pictorially alongside a number line e.g.:



Abstract number line showing three jumps of four.

$$3 \times 4 = 12$$



Multiplication

Concrete

Understand how to use times-tables facts flexibly.



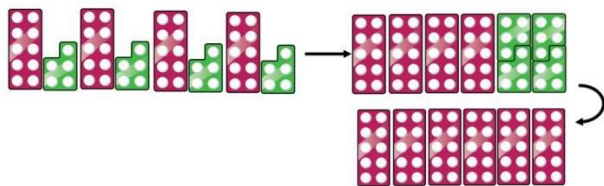
There are 6 groups of 4 pens.

There are 4 groups of 6 bread rolls.



I can use $6 \times 4 = 24$ to work out both totals.

Partition to multiply using Numicon, base 10 or Cuisenaire rods.
 4×15

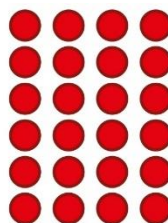
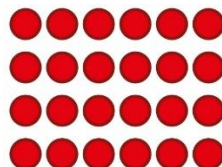


Pictorial

Understand how times-table facts relate to **commutativity**.

$$6 \times 4 = 24$$

$$4 \times 6 = 24$$



Abstract

Understand how times-table facts relate to commutativity.

I need to work out 4 groups of 7.

I know that $7 \times 4 = 28$

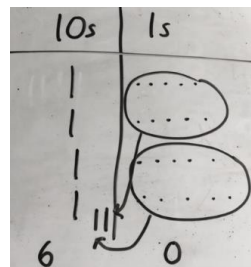
so, I know that

4 groups of 7 = 28

and

7 groups of 4 = 28.

Children to represent the concrete manipulatives pictorially.



Children to represent partitioning in a grid

$\times$	10	5
4	40	20

$$4 \times 10 = 40$$

$$4 \times 5 = 20$$

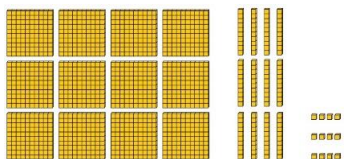
$$40 + 20 = 60$$

Multiplication

Concrete

Multiplying by 10, 100, 1000 etc.

Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.



3 groups of 4 ones is 12 ones.

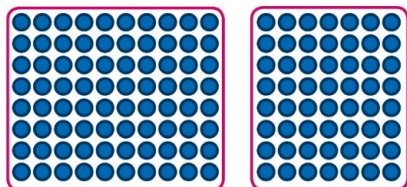
3 groups of 4 tens is 12 tens.

3 groups of 4 hundreds is 12 hundreds.

Multiplying up to 4-digit numbers by a single digit

Explore how to use partitioning to multiply efficiently.

$$8 \times 17 = ?$$



$$8 \times 10 = 80$$

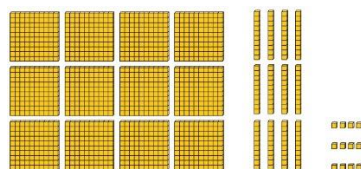
$$8 \times 7 = 56$$

$$80 + 56 = 136$$

$$\text{So, } 8 \times 17 = 136$$

Pictorial

Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.



$$3 \times 4 = 12$$

$$3 \times 40 = 120$$

$$3 \times 400 = 1,200$$

Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.

H	T	O
100	10 10 10 10 10	1 1 1
100	10 10 10 10 10	1 1 1
100	10 10 10 10 10	1 1 1
100	10 10 10 10 10	1 1 1
100	10 10 10 10 10	1 1 1

Abstract

Use known facts and understanding of place value and commutativity to multiply mentally.

$$4 \times 7 = 28$$

$$4 \times 70 = 280$$

$$40 \times 7 = 280$$

$$4 \times 700 = 2,800$$

$$400 \times 7 = 2,800$$

Use an area model and then add the parts.

	100	60	3
5	$100 \times 5 = 500$	$60 \times 5 = 300$	$3 \times 5 = 15$

Use a column multiplication, including any required exchanges.

$$\begin{array}{r} 136 \\ \times 6 \\ \hline 816 \\ \hline 23 \end{array}$$

Multiplication

Concrete

Multiplying 2-digit numbers by 2-digit numbers (And more)

Partition one number into 10s and 1s, then add the parts.

$$23 \times 15 = ?$$



$$23 \times 15 = 345$$

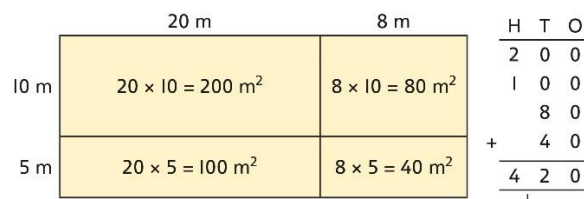


$$\begin{array}{r} \text{H T O} \\ 150 \\ 150 \\ + 45 \\ \hline 345 \end{array}$$

Pictorial

Use an area model and add the parts.

$$28 \times 15 = ?$$



$$28 \times 15 = 420$$

$$\begin{array}{r} \text{H T O} \\ 200 \\ 100 \\ 80 \\ + 40 \\ \hline 420 \end{array}$$

Abstract

Use column multiplication, ensuring understanding of place value at each stage.

$$\begin{array}{r} 34 \\ \times 27 \\ \hline 238 \\ 680 \\ \hline 2278 \end{array}$$

Use grid multiplication

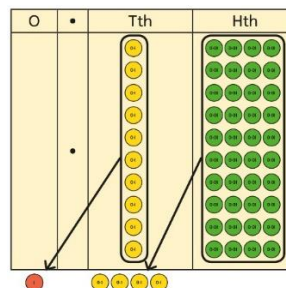
×	30	4
20	600	80
7	210	28

$$\begin{array}{r} 600 \\ 210 \\ + 28 \\ \hline 638 \end{array}$$

Multiplying decimals by 10, 100 and 1,000

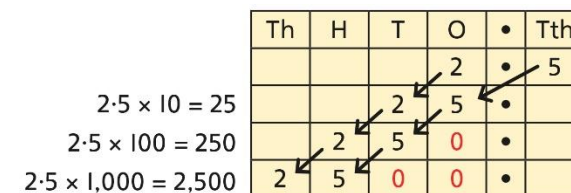
Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.

Represent multiplication by 10 as exchange on a place value grid.



$$0.14 \times 10 = 1.4$$

Understand how this exchange is represented on a place value chart.



$$\begin{array}{l} 2.5 \times 10 = 25 \\ 2.5 \times 100 = 250 \\ 2.5 \times 1,000 = 2,500 \end{array}$$

Division

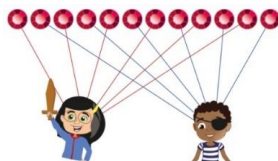
Division - Key Language

Share, equal group, divide, factor, ratio, half, quarter

(Careful with fraction language e.g. “*what is half of*” or “*find a half of*” not “*divide by half*”)

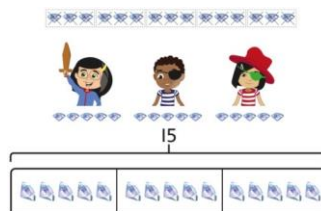
Concrete

Start with a whole and share into equal parts, one at a time.



*12 shared equally between 2.
They get 6 each.*

Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared

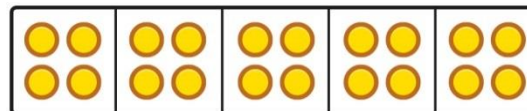


They get 5  each.

*15 shared equally between 3.
They get 5 each.*

Pictorial

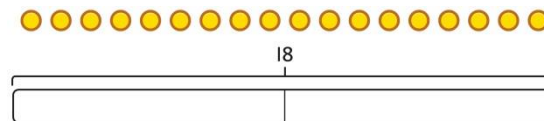
Represent the objects shared into equal parts using a bar model.



*20 shared into 5 equal parts.
There are 4 in each part.*

Abstract

Use a bar model to support understanding of the division.

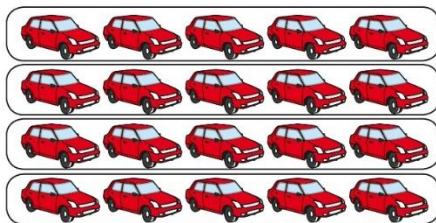


$$18 \div 2 = 9$$

Division

Concrete

Understand the relationship between multiplication facts and division.

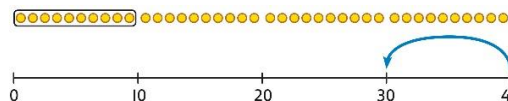


4 groups of 5 cars is 20 cars in total.

20 divided by 4 is 5.

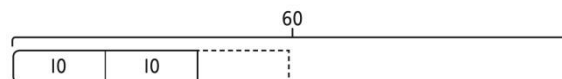
Pictorial

Link equal grouping with repeated subtraction and known times-table facts to support division.



40 divided by 4 is 10.

Use a bar model to support understanding of the link between times-table knowledge and division.



Abstract

Relate times-table knowledge directly to division.

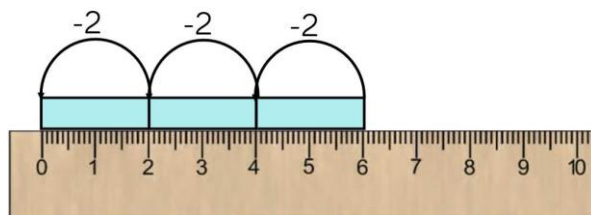
$1 \times 10 = 10$
 $2 \times 10 = 20$
 $3 \times 10 = 30$
 $4 \times 10 = 40$
 $5 \times 10 = 50$
 $6 \times 10 = 60$
 $7 \times 10 = 70$
 $8 \times 10 = 80$

I used the 10 times-table to help me.
 $3 \times 10 = 30$.

I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.

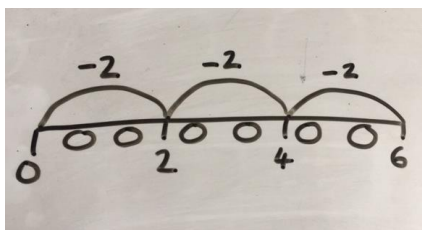
$3 \times 10 = 30$ so $30 \div 10 = 3$

Repeated subtraction using Cuisenaire rods above a ruler. $6 \div 2$

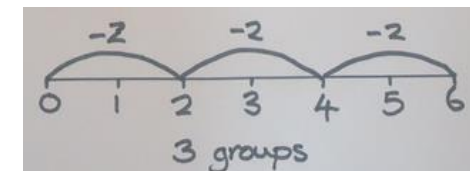


3 groups of 2

Children to represent repeated subtraction pictorially.



Abstract number line to represent the equal groups that have been subtracted.



Division

Concrete

Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.

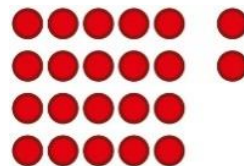


There are 13 sticks in total.

There are 3 groups of 4, with 1 remainder.

Pictorial

Use images to explain remainders.



$$22 \div 5 = 4 \text{ remainder } 2$$

Abstract

Understand that the remainder is what cannot be shared equally from a set.

$$22 \div 5 = ?$$

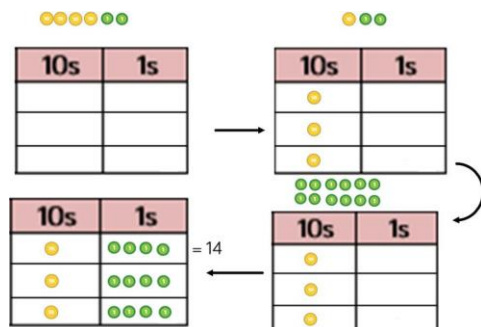
$$3 \times 5 = 15$$

$$4 \times 5 = 20$$

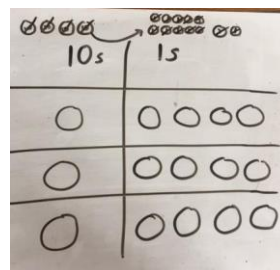
$$5 \times 5 = 25 \dots \text{this is larger than } 22$$

$$\text{So, } 22 \div 5 = 4 \text{ remainder } 2$$

Sharing using place value counters.



Children to represent the place value counters pictorially



Children to be able to make sense of the place value counters and write calculations to show the process.

$$42 \div 3$$

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

$$10 + 4 = 14$$

Division

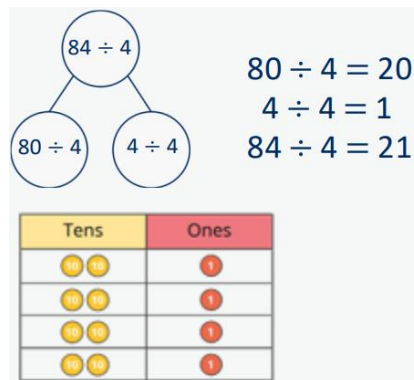
Concrete

Divide a 2 or 3-digit number by a 1-digit number

Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders

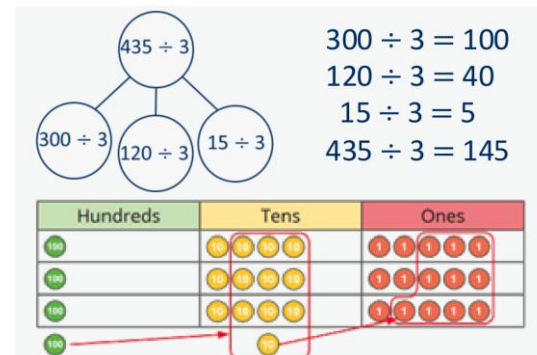
Pictorial

I can partition ... into ... tens and ... ones.



Abstract

I cannot share the hundreds/tens equally, so I need to exchange 1 ... for 10 ...



Divide numbers up to 4 digits by a 1-digit number

The short division method is introduced for the first time.

There are ... groups of ... hundreds/tens/ones/ in ...
I can exchange 1 ... for 10 ...

